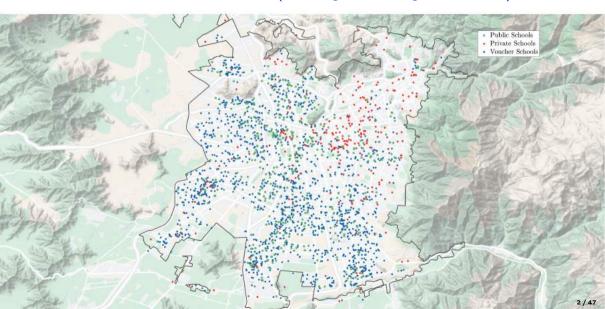
Biased Beliefs and Search in Education Markets

Claudia Allende, Patrick Agte, Adam Kapor, Christopher Neilson, Fernando Ochoa

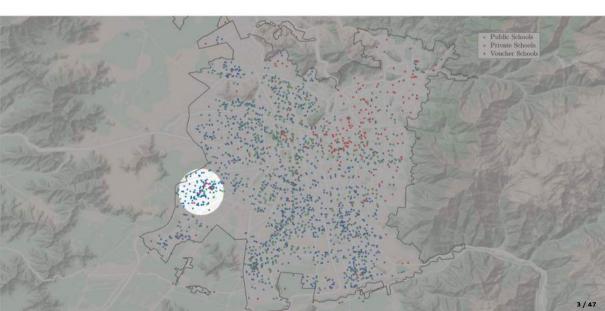
Stanford GSB; Princeton University; Yale University; New York University

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Urban Education Markets in Chile (Santiago, Kindergarden Level)



Zoom into a 2km Radius Area



Almost 100 Schools Offering K Among Which Families Can Choose



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- We ask: how do families' (inaccurate) beliefs/info interact with search costs to affect families' search, applications, and school assignments?

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 - 5 Set up and estimate model of search and demand + simulate counterfactuals.

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 - Caveat: larger welfare gains for full info than "info about x's".

Literature

- We are looking at "consumer search" and demand in a high stakes setting.
 - De Los Santos et al (2012; 2017) Dinerstein et al (2018); Hodgson Lewis (2022); Moraga-Gonzales et al (2022); ...
 - ▶ Health plan choice: Handel and Kolstad (2015), ...
- Providing information about "X's" of schools can affect applications:
 - Hastings Weinstein (2008); Mizala Urquiola (2013); Corcoran et al (2017, 2022); Andrabi Das Khwaja (2017); Allende Gallego Neilson (2019); Bergman Chan Kapor (2020)
- Giving info about admissions chances can affect apps and assignments.
 - ► Hoxby Turner (2013, 2015); Gurantz et al (2021); Ajayi Friedman Lucas (2022)
 - Search → admissions beliefs relevant, even under SPDA. (AKNZ 2022)
- This paper's contributions:
 - ▶ Novel data on search and beliefs + information experiments:
 - ⇒ provide direct evidence that inaccurate beliefs distort search decisions
 - Estimate demand w/ limited consideration (extending consideration-set approach (Goeree (2008)) to allow inaccurate perceptions of "known" options), imperfect info, rich prefs:
 - \implies quantify welfare and school-quality impacts of addressing misperceptions + search costs

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Mean Utility and Discoverability	δ_j, η_j	
Treatments, search activity: excluded from \hat{u}	w_{ijt}	

- π plays two roles:
 - ▶ $\pi_{ijt} < 0 \rightarrow$ student doesn't know j at all.

• Student $i \in \mathcal{I}$ chooses among schools $j \in J_i \subset J$ (schools within 5km).

$$\pi_{ijt} = z_{ij}\alpha^z + w_{ijt}\alpha^w + w_{ijt}^{rc}\alpha_i^{rc} + \eta_j + \nu_{ijt}$$
 (Awareness, time t)

$$\hat{u}_{ijt} = z_{ij}\beta^z + \hat{x}_{ii}^{rc}(\pi_{ijt})\beta_i^{rc} + \delta_i + \hat{x}_{ij}(\pi_{ijt})\gamma + \hat{\varepsilon}_{ij}(\pi_{ijt}),$$
 (Subj. EU, time t)

• \hat{u}_{ijt} : payoff from j given info π_{ijt} ; depends on real characteristics and on subjective beliefs

Distance	z_{ij}	
Observable quality/price index $\in \{1,\ldots,4\}^2$	$ imes_{ij}$	$\hat{x}_{ij}(\pi_{ijt})$
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Treatments, search activity: excluded from \hat{u}	w_{ijt}	

- π plays two roles:
 - ▶ π_{iit} < 0 → student doesn't know *j* at all.
 - ▶ $\pi_{ijt} > 1$ → more accurately perceive observables (x_{ij}) , match value (ε_{ij}) .

$$\pi_{ijt} = z_{ij}\alpha^{z} + w_{ijt}\alpha^{w} + w_{ijt}^{rc}\alpha_{i}^{rc} + \eta_{j} + \nu_{ijt}$$
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 (Subj. EU, time t)

$$t = 0$$
 Student *i* endowed with info (π_{i0}) , associated perceptions $(\hat{x}, \hat{\varepsilon}, \Omega)$

$$\pi_{ijt} = z_{ij}\alpha^z + w_{ijt}\alpha^w + w_{ijt}^{rc}\alpha_i^{rc} + \eta_j + \nu_{ijt}$$
 (Awareness, time t)

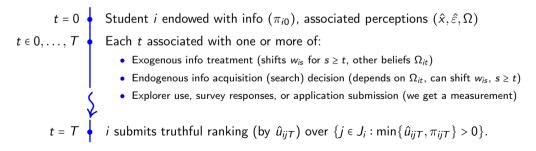
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 (Subj. EU, time t)

• Explorer use, survey responses, or application submission (we get a measurement)

$$t=0 \qquad \text{Student i endowed with info } (\pi_{i0}), \text{ associated perceptions } (\hat{x}, \hat{\varepsilon}, \Omega) \\ t \in 0, \dots, T \qquad \text{Each t associated with one or more of:} \\ \bullet \text{ Exogenous info treatment (shifts w_{is} for $s \geq t$, other beliefs Ω_{it})} \\ \bullet \text{ Endogenous info acquisition (search) decision (depends on Ω_{it}, can shift w_{is}, $s \geq t$)}$$

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where \hat{r} are subjective rejection probabilities, and $\hat{u}_{i1t} > \ldots > \hat{u}_{iMt} > 0$ WLoG.

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Continue if the expected gains from searching exceed the costs:

$$\hat{E}(\hat{U}'_{it}|\Omega_{it}) - \hat{U}_{it} > c_i(n)$$

where $c_i(n)$ depends on number of clicks (n), baseline characteristics $(\pi^0$, others), Ω_{it} is all current information and beliefs.

Model: Sequential Search

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* From previous slides: awareness (π) shifters w_{ijt} include indicator for having inspected j at $s \le t$

- Beliefs about admissions: optimism/pessimism and compression.
 - true rejection chance is rij
 - hh believes $\hat{r}_{ij} = \max\{\min\{o_{i0} + o_{i1}(r_{ij} o_{i0}) + \nu_{ij}^a, 1\}, 0\}.$

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▶ Beliefs about the distribution of match quality: Optimism/pessimism

$$\varepsilon_{ij} \sim N(\hat{\mu}, \hat{\sigma}^2)$$
, where the truth is $N(0, \sigma_{\varepsilon}^2)$

Outline

- Model
- Setting and interventions
- Data and descriptive analysis
- Estimation and counterfactuals

Chilean School Choice Process

- Chile uses a student-proposing deferred acceptance procedure for centralized assignment
- Single nationwide online platform
 - ▶ Pre-K to 12th grade
 - ▶ Public and Voucher schools ⇒ approximately 90% of total enrollment
 - Applicants concentrate on entry levels: Pre-K (23.50%), Kindergarten (7.89%), 1st grade (13.62%) and 9th grade (25%)
- Students allocated based on quotas and priorities.
- In 2021, 3,088,505 (85.17%) students enrolled in public and voucher schools
 - ⇒ Of these, 461,223 (14.93%) participated in the regular round

Interventions

- Personalized Search
 - Universe: Households w/ children entering the regular education system for the first time.
 - 3,948 participants, recruited from preschools.

Treatments:

- 1. Control: Access to explorer
- 2. Treatment 1: Access to explorer + Distribution
- 3. Treatment 2: Access to explorer + Distribution + Report Card + Highlight schools with p = 0, quality $\in \{3, 4\}$.

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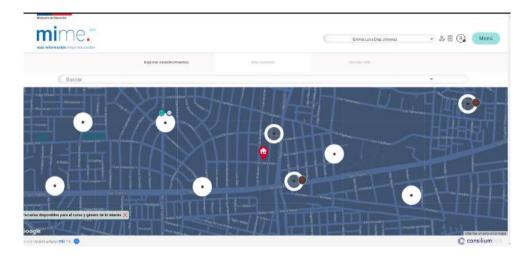
Treatments:

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- 2. Treatment 1: Access to explorer + Distribution
- Treatment 2: Access to explorer + Distribution + Report Card + Highlight schools with p = 0, quality $\in \{3, 4\}$.
- Personalized Feedback
 - ▶ Universe: Households with a valid SAE application one week before the end of main application period. Restrict to urban markets, grades {Pre-K, K, 1, 9}.
 - 162k participants, 45k of which have > 0 risk of non-assignment.
 - This paper: we restrict to intersection with search sample.

Treatments:

- Personalized feedback about schools in portfolio; risk warning; list of recommendations; access to explorer.
- Pure control (Whatsapp message)

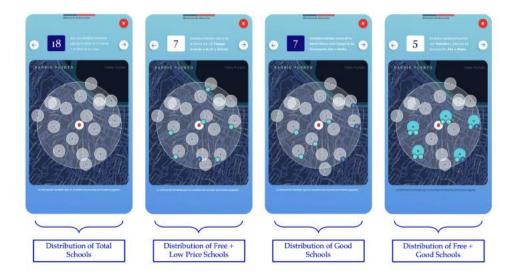
Treatments: School Explorer



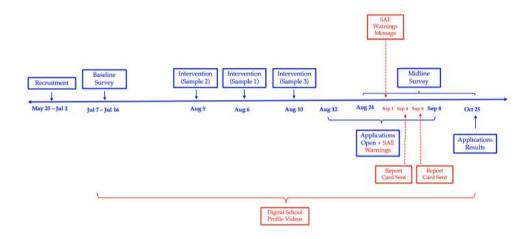
Treatments: Treatment 1

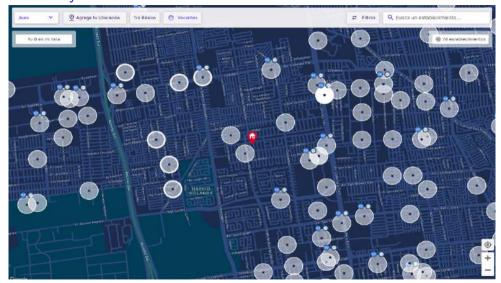


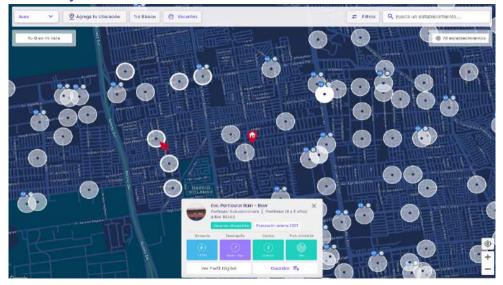
Treatments: Treatment 2

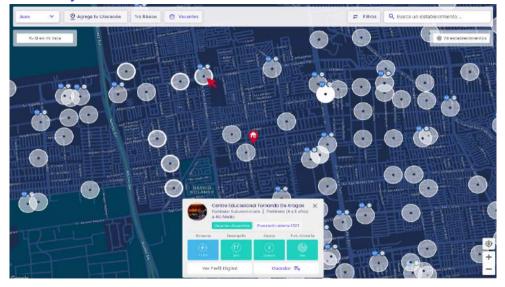


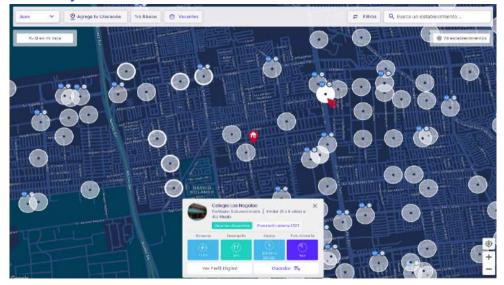
Timing Intervention 2021

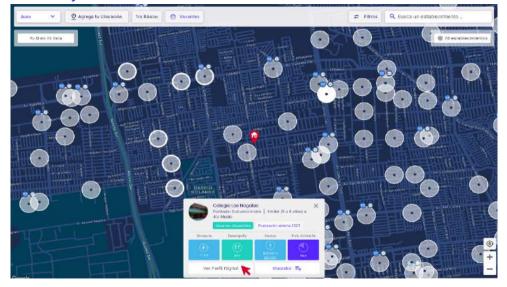


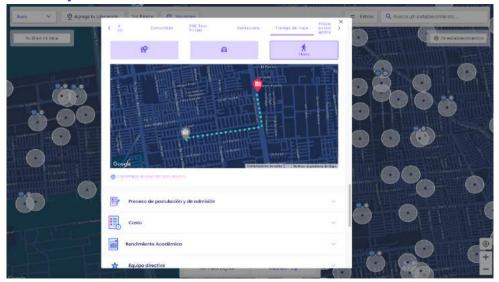


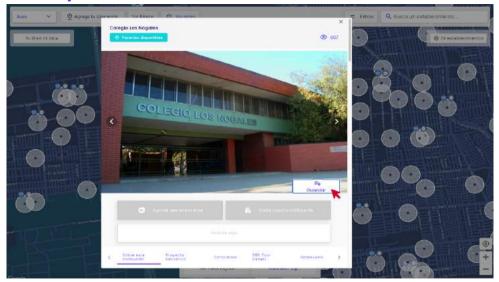












Personalized feedback



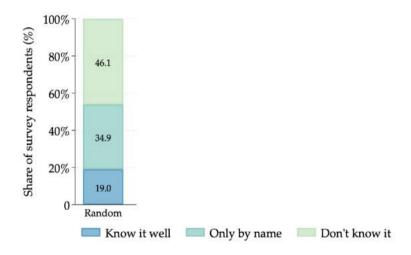




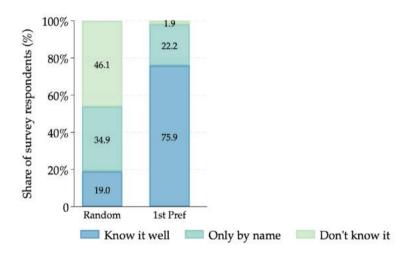
Outline

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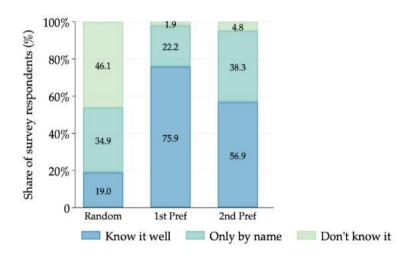
Fact 1a: households do not know all schools



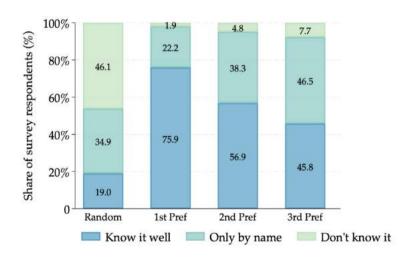
Fact 1b: First preference known well



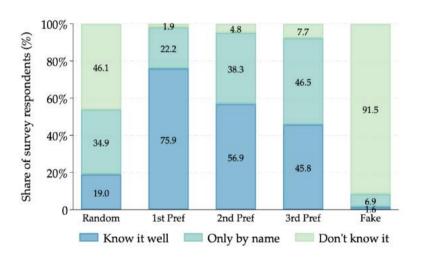
Fact 1c: Second preference known less well



Fact 1d: Third preference known less well



Fact 1e: Don't know fake school



Fact 2: Households overestimate quality and price of unknown schools

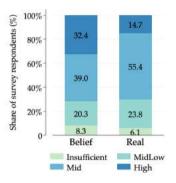


Figure 1: Quality

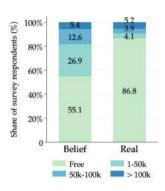
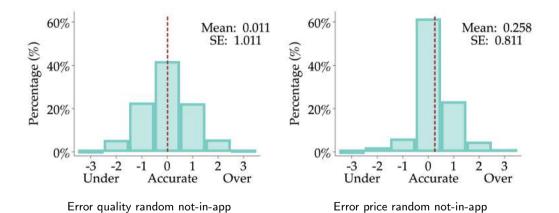


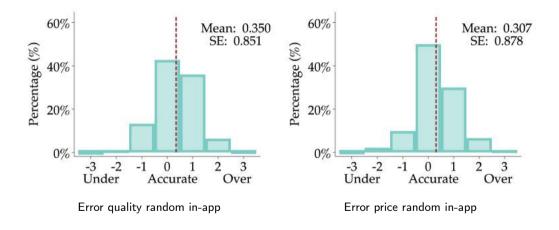
Figure 2: Price

▶ Quality index and value added

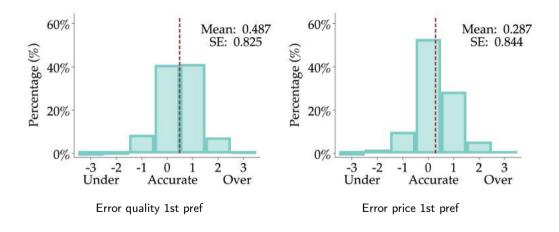
Fact 3a: Households also misinformed about price, quality of **known** schools



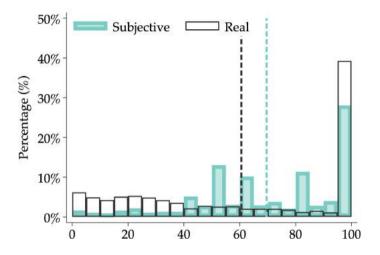
Fact 3b: Households overestimate quality of schools they apply to



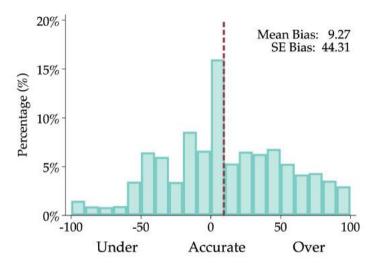
Fact 3c: Households overestimate quality of first-choice school



Fact 4: Households also mispredict admissions chances



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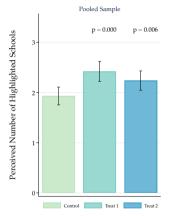


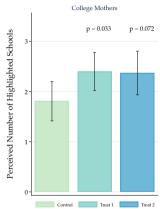
Empirical Strategy for Personalized Search Experiment

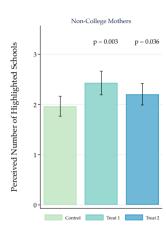
$$Y_i = \alpha + \beta_1 T 1_i + \beta_2 T 2_i + \lambda_i + \gamma X_i + \varepsilon_i.$$

- $T1_i, T2_i$: treatment status λ_i : strata fixed effect X_i : baseline controls (selected through double-lasso)
- Show separate results for college (23%) and non-college mothers (77%).

Treatment Affects Beliefs

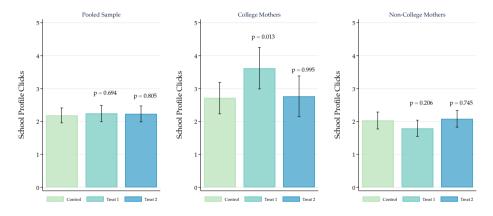






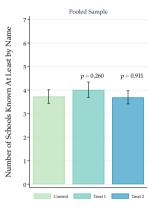
▶ Regression Table

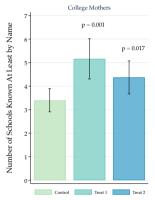
Treatment Increases Search for College Mothers

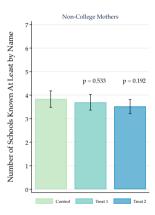


• Similar treatment effects in two follow-up experiments in Chile and DR. Details

Treatment Affects Knowledge for College Mothers

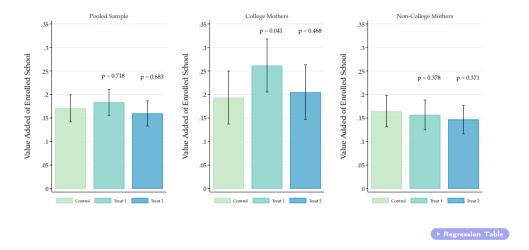






→ Regression Table

Treatment Affects Enrollment



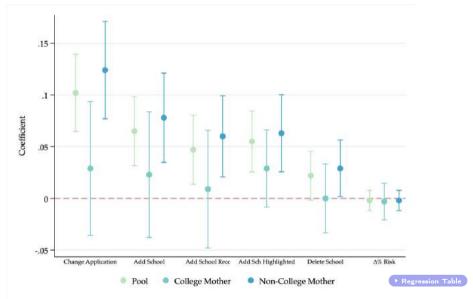
• Treatment 2 increases likelihood that 2nd ranked school in application is highlighted.

Empirical Strategy for Personalized Feedback Experiment

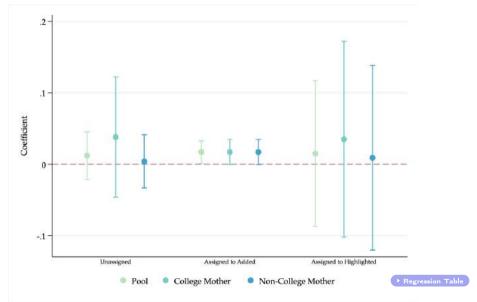
$$Y_i = \alpha + \beta T_i + \lambda_i + \gamma X_i + \varepsilon_i.$$

- T_i : treatment status λ_i : strata fixed effect X_i : baseline controls
- Use treatment assignment as instrument for opening feedback intervention.

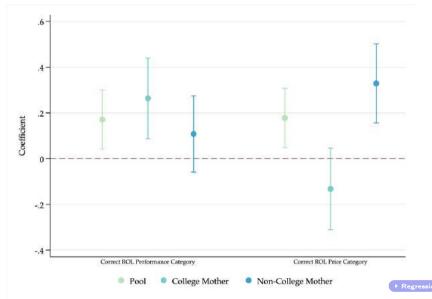
Feedback Treatment Affects Application



Feedback Treatment Affects Assignment



Feedback Treatment Affects Knowledge



Descriptive Analysis: Summary

- Households do not know all nearby schools.
 - ► In paper: high-quality schools (somewhat) more likely to be known at baseline ► Table
- Households hold inaccurate beliefs:
 - $\blacksquare F(price, quality)$ over schools they don't know
 - admissions chances
 - quality and price of "known" schools
 - ▶ In paper: rankings respond to subj. beliefs not truth ▶ Table
- Information treatments:
 - shift beliefs (all), search effort (college moms), apps and matches (VA, college moms)
 - ► Sample is balanced ► Table
 - ► Heterogeneity not driven by differences in choice sets or beliefs ► More
- Search activity:
 - occurs almost entirely in a short period after we prompt people Timing Search Actions
 - effort responds to subjective beliefs
 - stopping rule depends on history (i.e. search looks sequential)
 - clicks predict knowledge of schools, accurate beliefs, applications

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Empirics: preferences (u) and awareness (π)

We specialize to three levels of knowledge, "potential utilities":

$$\pi_{ijt} = z_{ij}\alpha^z + w_{ijt}\alpha^w + w_{ijt}^{rc}\alpha_i^{rc} + \eta_j + \nu_{ijt}$$
 (Awareness, time t)

$$\hat{u}_{ijt} = 1(\pi_{ijt} > 1)u_{ij}^h(\hat{x}_{ij}^h) + 1(0 < \pi_{ijt} \le 1)u_{ij}^l(\hat{x}_{ij}^l)$$
 (Subj. EU, time t)

Can know a school well $(\pi_{ijt} > 1)$, somewhat $(0 < \pi_{ijt} \le 1)$, or not at all $(\pi_{ijt} < 0)$.

Empirics: preferences (u) and awareness (π)

We specialize to three levels of knowledge, "potential utilities":

$$\pi_{ijt} = z_{ij}\alpha^z + w_{ijt}\alpha^w + w_{ijt}^{rc}\alpha_i^{rc} + \eta_j + \nu_{ijt}$$
 (Awareness, time t)

$$\hat{u}_{ijt} = 1(\pi_{ijt} > 1)u_{ii}^h(\hat{x}_{ij}^h) + 1(0 < \pi_{ijt} \le 1)u_{ij}^l(\hat{x}_{ij}^l)$$
 (Subj. EU, time t)

Can know a school well $(\pi_{ijt} > 1)$, somewhat $(0 < \pi_{ijt} \le 1)$, or not at all $(\pi_{ijt} < 0)$.

$$u_{ij}^{h}(\hat{x}_{ij}^{h}) = z_{ij}\beta^{z} + \hat{x}_{ij}^{h,rc}\beta_{i}^{rc} + \delta_{j} + \hat{x}_{ij}^{h}\gamma + \varepsilon_{ij}$$
 (Subj. EU, high info)

$$u_{ij}^{l}(\hat{x}_{ij}^{l}) = z_{ij}\beta^{z} + \hat{x}_{ij}^{l,rc}\beta_{i}^{rc} + \delta_{j} + \hat{x}_{ij}^{l}\gamma + \hat{E}(\varepsilon_{ij}|\tilde{\varepsilon}_{ij})$$
 (Subj. EU, low info)

$$\hat{x}_{ij}^{l} \sim \Gamma(\cdot|x_{j}), \quad \hat{x}_{ij}^{h} = (x_{j} \text{ w.p. } p^{h}, \text{ otherwise } \hat{x}_{ij}^{l})$$
 (Perceived "observables")

"know well" \implies better knowledge of match value, (stochastically) better signal of x.

Empirics: preferences (u) and awareness (π)

We specialize to three levels of knowledge, "potential utilities":

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$$\hat{u}_{ijt} = 1(\pi_{ijt} > 1)u_{ij}^h(\hat{x}_{ij}^h) + 1(0 < \pi_{ijt} \le 1)u_{ij}^l(\hat{x}_{ij}^l)$$
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Can know a school well $(\pi_{ijt} > 1)$, somewhat $(0 < \pi_{ijt} \le 1)$, or not at all $(\pi_{ijt} < 0)$.

$$\begin{aligned} u^h_{ij}(\hat{x}^h_{ij}) &= z_{ij}\beta^z + \hat{x}^{h,rc}_{ij}\beta^{rc}_i + \delta_j + \hat{x}^h_{ij}\gamma + \varepsilon_{ij} \\ u^l_{ij}(\hat{x}^l_{ij}) &= z_{ij}\beta^z + \hat{x}^{l,rc}_{ij}\beta^{rc}_i + \delta_j + \hat{x}^h_{ij}\gamma + \hat{E}(\varepsilon_{ij}|\tilde{\varepsilon}_{ij}) \\ \hat{x}^l_{ij} &\sim \Gamma(\cdot|x_j), \quad \hat{x}^h_{ij} &= (x_j \text{ w.p. } p^h, \text{ otherwise } \hat{x}^l_{ij}) \end{aligned} \qquad \text{(Subj. EU, low info)}$$

"know well" \implies better knowledge of match value, (stochastically) better signal of x.

- Correlated random effects: $(\eta_j, \delta_j)' \sim N((x_j \overline{\alpha}, x_j \overline{\beta})', \Sigma^{\eta \delta})$.
- Random coefficients: $\beta_i^{rc} \sim MVN(0, \Sigma^{rc}), \ \alpha_i \sim MVN(0, \Sigma^{\alpha rc}).$
- Post-search (exogenous) off-platform learning: $(\nu_{ii}^0, \dots, \nu_{ii}^T)' \sim N(\overline{\eta}, \Sigma^{\pi})$, with $\overline{\eta}_0 = 0$.
- Shock $\varepsilon_{ij} \sim N(0, \sigma_{\varepsilon}^2)$. If $\pi_{ijt} \in (0, 1)$, observe w/ normal noise; shrink to subj. prior.

Estimation Overview

We estimate the model in two steps:

- **I** Estimate $(u, \pi, \hat{x}, \beta_i^x)$, associated index and VCV params) via Gibbs sampler.
 - Data:
 - baseline (survey) ROL; administrative "just-before-feedback" and "final" ROLs
 - treatment assignments and responses; explorer "detail views";
 - 3 survey waves of: "how well do you know", perceived x's; 2 waves beliefs about F(x).
 - w: treatments, highlight, detail views. RC's on $(1, \text{dist}, \hat{x})$.
 - ▶ Normalizations: mean coef on distance = −1; $E(\varepsilon)$ = 0.
 - Include (and estimate) measurement error on every survey variable.
 - ID: use repeated within-person measurements of ROL, π , \hat{x} ; variation in treatment assignments and search outcomes.
- Estimate remaining parameters using optimality of search decisions.
 - Estimate admissions beliefs, "x" beliefs (Λ), (click probabilities | continue) via MLE.
 - Compute subjective expected utility of search at each history using these objects and results from (1).
 - W/ SEU of search in hand, estimate search cost distribution via SMLE.

Random Effects: Mean Utility (δ) and Discoverability (η)

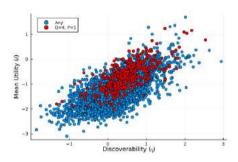


Figure 5: Non-College Mother

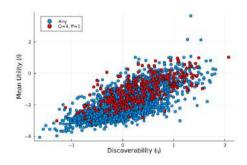


Figure 6: College Grad

Random Effects: Mean Utility (δ) and Discoverability (η)

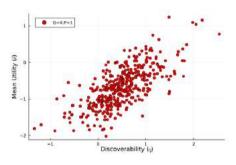


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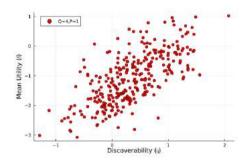


Figure 6: College Grad

We compare:

Baseline (as in data)

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- Provide accurate info about price, quality (i.e. $\hat{x} := x$), just before apps are due, taking awareness as given.

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 - ▶ This is a best-case "early" info intervention.
- In Full-info benchmark: $\hat{x} = x$ and $\pi_{ij}^T > 1$ for all (i,j) with dist_{ij} < 5km.
- We also estimate a specification in which we assume $\hat{x} = x$, consider "full-info benchmark" under that specification.

Main Results: Quality

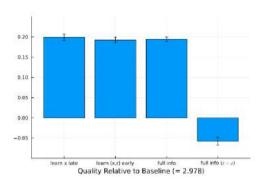


Figure 7: Non-College-Grad Mother

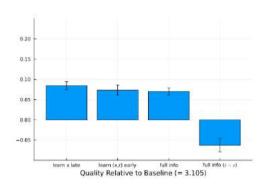


Figure 8: College Grad Mother

Main Results: Value Added

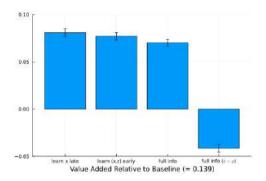


Figure 9: Non-College-Grad Mother

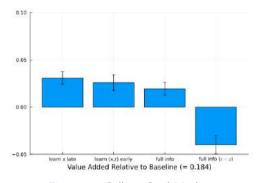


Figure 10: College Grad Mother

Main Results: Pr(Place)

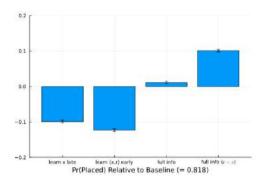


Figure 11: Non-College-Grad Mother

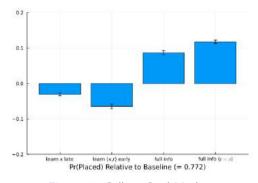


Figure 12: College Grad Mother

Main Results: Perceived Welfare

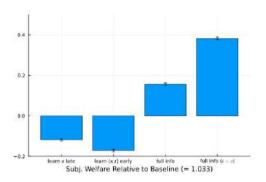


Figure 13: Non-College-Grad Mother

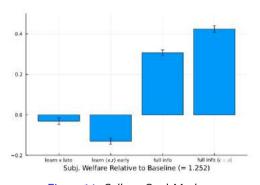


Figure 14: College Grad Mother

Main Results: Welfare

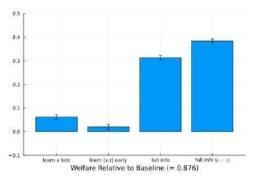


Figure 15: Non-College-Grad Mother

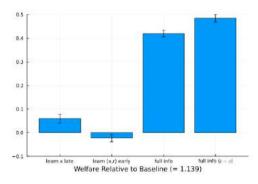


Figure 16: College Grad Mother

Search costs, biased/inaccurate beliefs interact

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Conclusions

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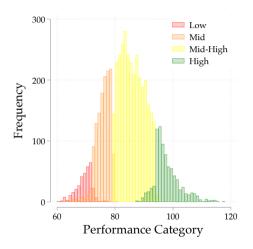
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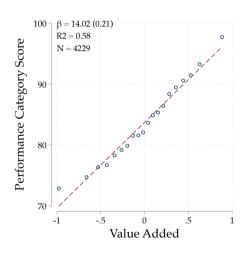
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- Recently concluded fieldwork in additional settings (Chile 9th-grade; DR).

Performance category and Value Added







Baseline: Better Schools Known (Slightly) Better

	Know Well	Know by Name	Don't Know
High Performance	23.33%	38.02%	38.65%
Medium Performance	18.45%	36.26%	45.28%
Med-Low Performance	11.82%	32.39%	55.79%
Insufficient Performance	9.37%	28.07%	62.56%

Table 1: Baseline Awareness Set I



Reported beliefs about p, q, not truth, predict rankings

		Partial I	Ranking	Regular Rou	ınd Ranking
		(1			2)
Distance		-0.000	(0.003)	-0.048**	(0.020)
	1	-0.306**	(0.119)	0.280	(0.188)
Perceived Price Category	3	-0.226*	(0.133)	-0.152	(0.249)
	4	-1.269***	(0.236)	-0.329	(0.502)
	1	0.052	(0.118)	-0.078	(0.200)
Real Price Category	3	0.166	(0.134)	0.284	(0.233)
	4	0.153	(0.216)	0.295	(0.459)
	1	-1.683***	(0.623)	-1.593	(1.091)
Perceived Performance	3	1.894***	(0.176)	0.232	(0.241)
	4	3.712***	(0.202)	1.023***	(0.276)
	1	-0.569**	(0.252)	0.020	(0.459)
Real Performance	3	0.099	(0.113)	-0.113	(0.185)
	4	0.226*	(0.127)	0.028	(0.216)
Public School		-0.344***	(0.112)	-0.050	(0.172)
Observations		3568		1199	

Notes. This table presents a rank-ordered logit choice model. Column (1) refers to the partial ranking we elicited at baseline with perceived price and quality from responses to the baseline survey. Column (2) refers to the ranking from application data from SAE Regular Round, with perceived price and quality from responses to the midline survey.



Balance Check Slides

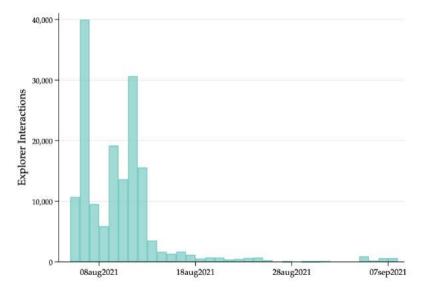
	Cor	ntrol	Treat	ment 1	Treat	ment 2			Cor	ntrol	Treat	ment 1	Treati	ment 2	
	Mean	St. Dev.	Coeff.	St. Err.	Coeff.	St. Err.	N		Mean	St. Dev.	Coeff.	St. Err.	Coeff.	St. Err.	N
	(1)	(2)	(3)	(4)	(5)	(6)	(7)		(1)	(2)	(3)	(4)	(5)	(6)	(7)
Panel A: Choice En	vironment	:						Panel C: Initial Know	wlege and	Beliefs					
N Schools (in SAE)	18.778	[8.903]	0.154	(0.427)	0.262	(0.433)	1,801	Satisfaction	5.144	[1.392]	0.053	(0.083)	0.017	(0.084)	1,679
N Schools (Any)	42.904	[17.580]	0.124	(0.895)	0.274	(0.894)	1,801	Pref 1 (Any)	0.911	[0.286]	-0.008	(0.017)	-0.008	(0.017)	1,801
N Highlighted (Any)	9.414	[4.785]	0.096	(0.264)	0.254	(0.260)	1,801	Pref 1 (HL)	0.490	[0.500]	0.044	(0.032)	0.026	(0.032)	1,402
								Perceived adm.	68.089	[25.839]	1.400	(1.538)	1.358	(1.533)	1,679
Panel B: Parent/Ch	ild Charac	cteristics						N Schools known A	3.608	[2.745]	-0.027	(0.158)	0.068	(0.154)	1,801
								N Schools known B	1.925	[2.126]	-0.038	(0.123)	-0.072	(0.120)	1,801
Child is female	0.483	[0.500]	0.043	(0.029)	0.040	(0.029)	1,801	Perceived N (2km)	6.803	[8.769]	-0.441	(0.420)	-0.882	(0.391)	1,801
Child's Birth Year	0.076	[0.541]	0.008	(0.031)	0.029	(0.031)	1,801	Perceived HL (2km)	2.086	[2.610]	0.124	(0.150)	-0.008	(0.144)	1,801
Mother Educ. HS	0.942	[0.234]	0.005	(0.012)	-0.006	(0.013)	1,798	SEP Eligible (Belief)	0.139	[0.346]	-0.021	(0.019)	-0.003	(0.020)	1,801
Mother Educ. Coll	0.249	[0.433]	0.000	(0.017)	-0.009	(0.017)	1,798	SEP Don't Know	0.702	[0.458]	-0.009	(0.027)	0.013	(0.026)	1,801
N younger siblings	1.141	[0.401]	0.023	(0.023)	0.008	(0.023)	1,801	Add info known	66.186	[30.149]	-2.104	(1.809)	-1.461	(1.787)	1,679
Has Disability	0.075	[0.263]	-0.007	(0.016)	-0.012	(0.016)	1,630	Add info unknown	55.858	[33.018]	1.071	(1.917)	0.454	(1.919)	1,679
Parent Sch. Staff	0.069	[0.255]	-0.010	(0.014)	-0.012	(0.014)	1,768	Would add school	0.821	[0.384]	0.005	(0.023)	0.013	(0.022)	1,679
SEP Household	0.373	[0.484]	-0.015	(0.014)	-0.018	(0.014)	1,781	Add sch. as pref 1	56.129	[29.431]	0.633	(1.808)	-0.084	(1.746)	1,679
								Add sch. blw last	66.264	[27.196]	1.109	(1.624)	-0.297	(1.612)	1,679

Heterogeneity Not Driven by Different Choice Environments or Beliefs

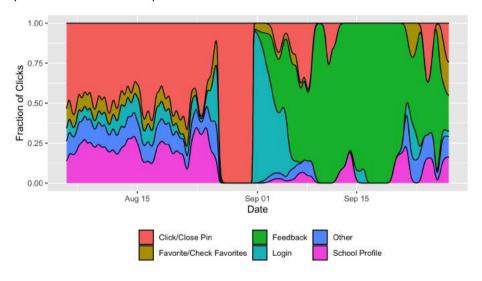
	Number of School Pin Clicks	Number of Highlighted School Pin Clicks	Value Added of Enrolled School
	(1)	(2)	(3)
Treatment 1 × College Mother	4.561**	1.461**	0.114**
	(2.110)	(0.708)	(0.047)
Treatment 1 \times Non-SEP	0.946	0.448	0.002
	(1.153)	(0.445)	(0.039)
Treatment 1 \times Below-Median Perceived Admin. Chances	1.203	0.092	0.017
	(1.353)	(0.470)	(0.036)
Treatment $1 \times \text{Number of Available Schools}$	0.063	0.014	0.002
	(0.047)	(0.018)	(0.001)
Treatment $1 \times Perceived Number of Available Schools$	-0.064	0.026	0.001
	(0.178)	(0.064)	(0.003)
Treatment $1 \times \text{Number of Available Highlighted Schools}$	-0.100	0.025	-0.005
	(0.173)	(0.066)	(0.005)
Treatment 1 \times Perceived Number of Available Highlighted Schools	0.377	0.146	0.000
	(0.277)	(0.101)	(800.0)
Observations	3,001	3,001	2,744



Almost all explorer use is just after we prompt households



Late explorer use is in response to "feedback" RCT





Selected estimates - Quality Distortion Function

Table 2: Non-College-Grad Mothers

subj. quality	true quality							
	1	2	3	4				
1	0.084 (0.017)	0.015 (0.003)	0.001 (0.001)	0.002 (0.001)				
2	0.364 (0.026)	0.291 (0.014)	0.109 (0.004)	0.054 (0.007)				
3	0.462 (0.029)	0.568 (0.012)	0.605 (0.01)	0.434 (0.014)				
4	0.089 (0.015)	0.126 (0.01)	0.285 (0.008)	0.51 (0.013)				

Table 3: College-Grad Mothers

subj. quality	true quality								
	1	2	3	4					
1	0.119 (0.085)	0.035 (0.017)	0.007 (0.005)	0.004 (0.004)					
2	0.478 (0.072)	0.451 (0.052)	0.187 (0.019)	0.085 (0.024)					
3	0.349 (0.096)	0.467 (0.04)	0.615 (0.025)	0.425 (0.031)					
4	0.053 (0.024)	0.047 (0.014)	0.191 (0.014)	0.485 (0.035)					

Main Results: Distance

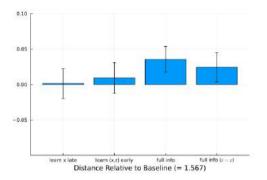


Figure 17: Non-College-Grad Mother

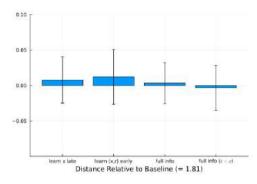


Figure 18: College Grad Mother

Main Results: Price

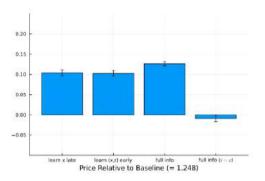


Figure 19: Non-College-Grad Mother

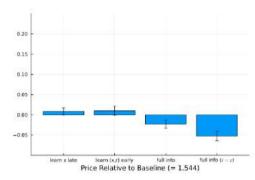


Figure 20: College Grad Mother

Main Results: Table

Table 4: Non-College-Grad Mothers

	EU	Place	E(rank)	Distance	Price	Quality	VA
baseline	0.877 (0.01)	0.818 (0.0)	1.447 (0.0)	1.567 (0.0)	1.248 (0.0)	2.978 (0.0)	0.139 (0.0)
learn x late	0.939 (0.011)	0.718 (0.006)	1.454 (0.008)	1.568 (0.021)	1.351 (0.007)	3.178 (0.008)	0.22 (0.004)
learn (x,r) early	0.896 (0.011)	0.693 (0.006)	1.44 (0.008)	1.577 (0.02)	1.35 (0.007)	3.171 (0.007)	0.217 (0.004)
full info benchmark	1.191 (0.013)	0.828 (0.006)	1.54 (0.009)	1.604 (0.021)	1.375 (0.007)	3.173 (0.009)	0.21 (0.004)
baseline ($\hat{x} = x$)	1.115 (0.035)						
full info ($\hat{x} = x$)	1.475 (0.061)	0.917 (0.004)	1.477 (0.006)	1.588 (0.014)	1.24 (0.006)	2.922 (0.008)	0.099 (0.005)

Table 5: College-Grad Mothers

EU	Place	E(rank)	Distance	Price	Quality	VA
1.134 (0.028)	0.772 (0.0)	1.703 (0.0)	1.81 (0.0)	1.544 (0.0)	3.105 (0.0)	0.184 (0.0)
1.193 (0.037)	0.74 (0.005)	1.684 (0.01)	1.817 (0.031)	1.553 (0.012)	3.192 (0.011)	0.216 (0.007)
1.111 (0.033)	0.706 (0.007)	1.64 (0.012)	1.82 (0.037)	1.554 (0.014)	3.181 (0.014)	0.211 (0.009)
1.555 (0.028)	0.858 (0.005)	1.792 (0.015)	1.814 (0.031)	1.523 (0.014)	3.178 (0.017)	0.204 (0.01)
1.171 (0.046)						
1.64 (0.061)	0.889 (0.005)	1.742 (0.021)	1.798 (0.03)	1.492 (0.015)	3.04 (0.019)	0.145 (0.01)
	1.134 (0.028) 1.193 (0.037) 1.111 (0.033) 1.555 (0.028) 1.171 (0.046)	1.134 (0.028) 0.772 (0.0) 1.193 (0.037) 0.74 (0.005) 1.111 (0.033) 0.706 (0.007) 1.555 (0.028) 0.858 (0.005) 1.171 (0.046)	1.134 (0.028) 0.772 (0.0) 1.703 (0.0) 1.193 (0.037) 0.74 (0.005) 1.684 (0.01) 1.111 (0.033) 0.706 (0.007) 1.64 (0.012) 1.555 (0.028) 0.858 (0.005) 1.792 (0.015) 1.171 (0.046)	1.134 (0.028) 0.772 (0.0) 1.703 (0.0) 1.81 (0.0) 1.193 (0.037) 0.74 (0.005) 1.684 (0.01) 1.817 (0.031) 1.111 (0.033) 0.706 (0.007) 1.64 (0.012) 1.82 (0.037) 1.555 (0.028) 0.858 (0.005) 1.792 (0.015) 1.814 (0.031) 1.171 (0.046)	1.134 (0.028) 0.772 (0.0) 1.703 (0.0) 1.81 (0.0) 1.544 (0.0) 1.193 (0.037) 0.74 (0.005) 1.684 (0.01) 1.817 (0.031) 1.553 (0.012) 1.111 (0.033) 0.706 (0.007) 1.64 (0.012) 1.82 (0.037) 1.554 (0.014) 1.555 (0.028) 0.858 (0.005) 1.792 (0.015) 1.814 (0.031) 1.523 (0.014) 1.171 (0.046)	1.134 (0.028) 0.772 (0.0) 1.703 (0.0) 1.81 (0.0) 1.544 (0.0) 3.105 (0.0) 1.193 (0.037) 0.74 (0.005) 1.684 (0.01) 1.817 (0.031) 1.553 (0.012) 3.192 (0.011) 1.111 (0.033) 0.706 (0.007) 1.64 (0.012) 1.82 (0.037) 1.554 (0.014) 3.181 (0.014) 1.555 (0.028) 0.858 (0.005) 1.792 (0.015) 1.814 (0.031) 1.523 (0.014) 3.178 (0.017) 1.171 (0.046)